

展開と因数分解 [乗法公式を利用した展開(1)]

乗法公式(1)

乗法公式

代表的な展開をまとめたもの

$$[1] (x + a)(x + b) = x^2 + \underset{\text{和}}{(a + b)}x + \underset{\text{積}}{ab}$$

<例> $(x + 2)(x + 3) = x^2 + (2 + 3)x + 2 \times 3$
 $= x^2 + 5x + 6$

$$(x + 3)(x - 5) = (x + 3)\{x + (-5)\} \quad \begin{matrix} \text{※負の数の加法とし、} \\ \text{乗法公式を使用} \end{matrix}$$
$$= x^2 + \{3 + (-5)\}x + 3 \times (-5)$$
$$= x^2 - 2x - 15$$

$$(x - 4)(x - 3) = \{x + (-4)\}\{x + (-3)\}$$
$$= x^2 + \{(-4) + (-3)\}x + (-4) \times (-3)$$
$$= x^2 - 7x + 12$$

<確認問題>

次の式を展開せよ。

(1) $(x + 4)(x + 5)$

(6) $(x + \frac{1}{2})(x + \frac{1}{3})$

(2) $(x + 10)(x + 11)$

(7) $(x + 0.1)(x - 0.2)$

(3) $(x + 5)(x - 7)$

(4) $(x - 2)(x + 6)$

(8) $(x + \frac{1}{3})(x - \frac{1}{4})$

(5) $(x - 2)(x - 3)$

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乗法公式(1)

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代表的な展開をまとめたもの

$$[1] (x + a)(x + b) = x^2 + (a + b)x + ab$$

↑ 和 ↑ 積

<例> $(x + 2)(x + 3) = x^2 + (2 + 3)x + 2 \times 3$
 $= x^2 + 5x + 6$

$$(x + 3)(x - 5) \stackrel{\text{※}}{=} (x + 3)\{x + (-5)\} \quad \begin{array}{l} \text{※負の数の加法とし、} \\ \text{乗法公式を使用} \end{array}$$
$$\stackrel{\text{※}}{=} x^2 + \{3 + (-5)\} x + 3 \times (-5)$$
$$= x^2 - 2x - 15$$

$$(x - 4)(x - 3) = \{x + (-4)\} \{x + (-3)\}$$
$$= x^2 + \{(-4) + (-3)\} x + (-4) \times (-3)$$
$$= x^2 - 7x + 12$$

<確認問題>

次の式を展開せよ。

(1) $(x + 4)(x + 5)$

$$(x + 4)(x + 5) = x^2 + (4 + 5)x + 4 \times 5$$
$$= x^2 + 9x + 20$$

(2) $(x + 10)(x + 11)$

$$(x + 10)(x + 11) = x^2 + (10 + 11)x + 10 \times 11$$
$$= x^2 + 21x + 110$$

(3) $(x + 5)(x - 7)$

$$(x + 5)(x - 7) = (x + 5)\{x + (-7)\}$$
$$= x^2 + \{5 + (-7)\} x + 5 \times (-7)$$
$$= x^2 - 2x - 35$$

(4) $(x - 2)(x + 6)$

$$(x - 2)(x + 6) = \{x + (-2)\} (x + 6)$$
$$= x^2 + \{(-2) + 6\} x + (-2) \times 6$$
$$= x^2 + 4x - 12$$

(5) $(x - 2)(x - 3)$

$$(x - 2)(x - 3) = \{x + (-2)\} \{x + (-3)\}$$
$$= x^2 + \{(-2) + (-3)\} x + (-2) \times (-3)$$
$$= x^2 - 5x + 6$$

(6) $(x + \frac{1}{2})(x + \frac{1}{3})$

$$\left(x + \frac{1}{2}\right) \left(x + \frac{1}{3}\right) = x^2 + \left(\frac{1}{2} + \frac{1}{3}\right) x + \frac{1}{2} \times \frac{1}{3}$$
$$= x^2 + \frac{5}{6}x + \frac{1}{6}$$

(7) $(x + 0.1)(x - 0.2)$

$$(x + 0.1)(x - 0.2) = (x + 0.1)\{x + (-0.2)\}$$
$$= x^2 + \{0.1 + (-0.2)\} x + 0.1 \times (-0.2)$$
$$= x^2 - 0.1x - 0.02$$

(8) $(x + \frac{1}{3})(x - \frac{1}{4})$

$$\left(x + \frac{1}{3}\right) \left(x - \frac{1}{4}\right) = \left(x + \frac{1}{3}\right) \left\{x + \left(-\frac{1}{4}\right)\right\}$$
$$= x^2 + \left\{\frac{1}{3} + \left(-\frac{1}{4}\right)\right\} x + \frac{1}{3} \times \left(-\frac{1}{4}\right)$$
$$= x^2 + \frac{1}{12}x - \frac{1}{12}$$